

Advanced Data Structures

The heap, deque, tree, and graph operations you actually write in an interview, with the time complexity that explains why.

1 HEAP *The smallest (or largest) item, ready in $O(1)$, whenever you do not need the rest sorted.*

OPERATION	SYNTAX	TIME
Build	<code>heapq.heapify(heap)</code>	$O(n)$
Push	<code>heapq.heappush(heap, x)</code>	$O(\log n)$
Pop	<code>heapq.heappop(heap)</code>	$O(\log n)$
Peek	<code>heap[0]</code>	$O(1)$
Max-heap push	<code>heappush(heap, (-x, item))</code>	$O(\log n)$

Tuples compare left to right, so two equal priorities fall through to comparing the second value, and a `TypeError` follows if that value cannot be ordered, like a dict. Push a counter in the middle, (priority, count, item), so the tie never reaches it.

2 DEQUE *A queue or a stack, whichever end you need $O(1)$ at, without two different classes to remember.*

OPERATION	SYNTAX	TIME
Append (right)	<code>dq.append(x)</code>	$O(1)$
Append (left)	<code>dq.appendleft(x)</code>	$O(1)$
Pop (right)	<code>dq.pop()</code>	$O(1)$
Pop (left)	<code>dq.popleft()</code>	$O(1)$
Peek	<code>dq[0]</code> / <code>dq[-1]</code>	$O(1)$

A list only tracks one end efficiently, so popping from the front means sliding every remaining item over, an $O(n)$ cost. A deque tracks both ends directly, so `popleft()` finishes in $O(1)$ no matter how long the queue is.

3 TREE *Parent and child links you walk top-down, one level or one branch at a time.*

OPERATION	SYNTAX	TIME
Node	<code>TreeNode(value)</code>	$O(1)$
Search (any tree)	<code>search_value(root, x)</code>	$O(n)$
Search (BST, avg)	<code>search_value(root, x)</code>	$O(\log n)$
BFS (level order)	<code>queue = deque([root])</code>	$O(n)$
DFS (recursive)	<code>dfs(node.left); dfs(node.right)</code>	$O(n)$

BFS holds a whole level in its queue at once, $O(w)$ space for the widest level. DFS only holds the current branch, $O(h)$ space for the height. A wide, shallow tree favors DFS; a deep, narrow one favors BFS.

4 GRAPH *Nodes and edges you look up by key, not by index, an adjacency list first.*

OPERATION	SYNTAX	TIME
Build	<code>adj_list = defaultdict(list)</code>	$O(1)$
Add edge	<code>adj_list[u].append(v)</code>	$O(1)$
Neighbors	<code>adj_list[u]</code>	$O(1)$
Visited check	<code>u in visited</code>	$O(1)$
Traversal	<code>bfs(adj_list, start)</code>	$O(n + e)$

A tree only has one path in; a graph can loop back on itself. Skip the visited set and a cycle spins the traversal forever, so mark a node visited the moment you enqueue or recurse into it, not once you get around to processing it.